CRYPTOEXPERTS

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Security of Masked Implementations Sonia Belaïd

LatinCrypt 2019









Black-box cryptanalysis:

 $\mathscr{A} \leftarrow (m, c)$





- Black-box cryptanalysis:
- Side-channel analysis:

 $\mathcal{A} \leftarrow (m, c)$ $\mathcal{A} \leftarrow (m, c, \mathcal{L})$





- Black-box cryptanalysis:
- Side-channel analysis:

 $\mathcal{A} \leftarrow (m, c)$ $\mathcal{A} \leftarrow (m, c, \mathcal{L})$



Overview of this talk

Masking Countermeasure

- Definition and implementation
- Leakage Models
 - Definitions, pros, and cons
 - Verification of Small Implementations
 - Example of tools to verify small implementations

Composition

How to compose small implementations into larger secure ones



Masking Countermeasure





Problem: the leakage is key-dependent





Problem: the leakage is key-dependent

Solution: Masking (make the leakage random)





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for each sensitive value $v \leftarrow f(p, k)$





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Solution: Masking (make the leakage random)

for each sensitive value $v \leftarrow f(p, k)$

$$v_1 \leftarrow \$ \qquad v_2 \leftarrow \$ \qquad \cdots \qquad v_{n-1} \leftarrow \$$$





Problem: the leakage is key-dependent

Solution: Masking (make the leakage random)

for each sensitive value $v \leftarrow f(p, k)$

$$v_0 \leftarrow v \oplus \left(\bigoplus_{i=1}^{n-1} v_i \right) \qquad v_1 \leftarrow \$ \qquad v_2 \leftarrow \$ \qquad \cdots \qquad v_{n-1} \leftarrow \$$$

Masking in Practice

Masking linear operations

 $z \leftarrow x \oplus y$

$$x = x_0 \oplus x_1 \oplus \ldots \oplus x_{n-1}$$

$$y = y_0 \oplus y_1 \oplus \dots \oplus y_{n-1}$$

Masking in Practice

Masking linear operations

$$z \leftarrow x \oplus y$$

$$x = x_0 \oplus x_1 \oplus \dots \oplus x_{n-1}$$

$$y = y_0 \oplus y_1 \oplus \dots \oplus y_{n-1}$$

$$\mathbf{z} = (x_0 \oplus y_0, x_1 \oplus y_1, \dots, x_{n-1} \oplus y_{n-1})$$



Masking in Practice

Masking linear operations

$$z \leftarrow x \oplus y$$

$$x = x_0 \oplus x_1 \oplus \dots \oplus x_{n-1}$$

$$y = y_0 \oplus y_1 \oplus \dots \oplus y_{n-1}$$

$$\mathbf{z} = (x_0 \oplus y_0, x_1 \oplus y_1, \dots, x_{n-1} \oplus y_{n-1})$$

Masking non linear operations

Cannot be done share by share

for
$$i = 0$$
 to t
for $j = i + 1$ to t
 $r_{i,j} \leftarrow \$$
 $r_{j,i} \leftarrow (r_{i,j} \oplus x_i y_j) \oplus x_j y_i$
for $i = 0$ to t
 $z_i \leftarrow x_i y_i$
for $j = 0$ to t , $j \neq i$
 $z_i \leftarrow z_i \oplus r_{i,j}$

Leakage Models



Security of an implementation

How to evaluate the security of an implementation?



Security of an implementation

How to evaluate the security of an implementation?

- Integrate it on a device and try to attack it
 - Not always possible





Security of an implementation

How to evaluate the security of an implementation?

- Integrate it on a device and try to attack it
 - Not always possible



Model the leakage and prove its security or exhibit an attack





Noisy Leakage Model



Leakage

- Every variable leaks
- Leakage = noisy function of the value

S. Chari, C. S. Jutla, J. R. Rao, and P. Rohatgi. Towards sound approaches to counteract power- analysis attacks. CRYPTO'99

E. Prouff and M. Rivain. Masking against side-channel attacks: A formal security proof. EUROCRYPT 2013



Random Probing Model



Leakage

- Every variable leaks with probability p
- Leakage = exact value



Probing Model

Leakage

- Only t variables leak in the implementation
- Leakage = exact value

Security in the t-probing model

Implementation such that any set of t intermediate variables is independent from the secret

ExpReal(\mathcal{A}, C):ExpSim($\mathcal{A}, \mathcal{S}, C$):1. $(\mathcal{P}, x_1, \dots, x_n) \leftarrow \mathcal{A}()$ 1. $(\mathcal{P}, x_1, \dots, x_n) \leftarrow \mathcal{A}()$ 2. $[x_1] \leftarrow \operatorname{Enc}(x_1), \dots, [x_n] \leftarrow \operatorname{Enc}(x_n)$ 1. $(\mathcal{P}, x_1, \dots, x_n) \leftarrow \mathcal{A}()$ 3. $(v_1, \dots, v_t) \leftarrow C([x_1], \dots, [x_n])_{\mathcal{P}}$ 2. $(v_1, \dots, v_t) \leftarrow \mathcal{S}(\mathcal{P})$ 4. Return (v_1, \dots, v_t) 3. Return (v_1, \dots, v_t)

Y. Ishai, A. Sahai, and D. Wagner. Private circuits: Securing hardware against probing attacks. CRYPTO 2003





Reductions



realism



Reductions



realism

A. Duc, S. Dziembowski, and S. Faust. Unifying leakage models: From probing attacks to noisy leakage. EUROCRYPT 2014



Verification of Small Implementations



Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret

2 shares I-probing secure? function example(a_0, a_1, b_0, b_1) $r \leftarrow \$$ $u \leftarrow a_0 \cdot b_0$ $c_0 \leftarrow u \oplus r$ $v \leftarrow a_1 \cdot b_1$ $x \leftarrow a_0 \cdot b_1$ $w \leftarrow v \oplus x$ $y \leftarrow w \oplus r$ $z \leftarrow a_1 \cdot b_0$ $c_1 \leftarrow y \oplus z$ return (c_0, c_1)



Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret

Independent from secrets?

function example(
$$a_0, a_1, b_0, b_1$$
)
 $r \leftarrow \$$
 $u \leftarrow a_0 \cdot b_0$
 $c_0 \leftarrow u \oplus r$
 $v \leftarrow a_1 \cdot b_1$
 $x \leftarrow a_0 \cdot b_1$
 $\overleftrightarrow{w} \leftarrow v \oplus x$
 $y \leftarrow w \oplus r$
 $z \leftarrow a_1 \cdot b_0$
 $c_1 \leftarrow y \oplus z$
return (c_0, c_1)



Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret

function example(a_0, a_1, b_0, b_1) $r \leftarrow \$$ $u \leftarrow a_0 \cdot b_0$ Independent from secrets? $c_0 \leftarrow u \oplus r$ $w = v \oplus x$ $v \leftarrow a_1 \cdot b_1$ $w = a_1 \cdot b_1 \oplus a_0 \cdot b_1$ $x \leftarrow a_0 \cdot b_1$ $w = a \cdot b_1$ $w \leftarrow v \oplus x$ $y \leftarrow w \oplus r$ $z \leftarrow a_1 \cdot b_0$ $c_1 \leftarrow y \oplus z$ return (c_0, c_1)



Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret

function example($a_0, a_1, a_2, b_0, b_1, b_2$)

3 shares

$$r_{00}, r_{01}, r_{02}, r_{12} \leftarrow \$$$

$$t \leftarrow a_0 \cdot b_0$$

$$c_0 \leftarrow t \oplus r_{00}$$

$$t \leftarrow a_0 \cdot b_1$$

$$t \leftarrow t \oplus r_{01}$$

$$c_0 \leftarrow c_0 \oplus t$$

$$t \leftarrow a_0 \cdot b_2$$

$$t \leftarrow t \oplus r_{02}$$

$$c_0 \leftarrow c_0 \oplus t$$

$$t \leftarrow a_1 \cdot b_0$$

$$c_1 \leftarrow t \oplus r_{01}$$

$$t \leftarrow a_1 \cdot b_1$$

$$c_1 \leftarrow c_1 \oplus t$$
....
return (c_0, c_1, c_2)



Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret

function example($a_0, a_1, a_2, b_0, b_1, b_2$)

3 shares 33 intermediate variables $\binom{33}{2} = 528$ couples to verify

$$\begin{aligned} r_{00}, r_{01}, r_{02}, r_{12} \leftarrow \$ \\ t \leftarrow a_0 \cdot b_0 \\ c_0 \leftarrow t \oplus r_{00} \\ t \leftarrow a_0 \cdot b_1 \\ t \leftarrow t \oplus r_{01} \\ c_0 \leftarrow c_0 \oplus t \\ t \leftarrow a_0 \cdot b_2 \\ t \leftarrow t \oplus r_{02} \\ c_0 \leftarrow c_0 \oplus t \\ t \leftarrow a_1 \cdot b_0 \\ c_1 \leftarrow t \oplus r_{01} \\ t \leftarrow a_1 \cdot b_1 \\ c_1 \leftarrow c_1 \oplus t \\ \dots \end{aligned}$$
return (c_0, c_1, c_2)



Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret

function example($a_0, a_1, a_2, b_0, b_1, b_2$)

	$r_{00}, r_{01}, r_{02}, r_{12} \leftarrow \$$
3 shares	$t \leftarrow a_0 \cdot b_0$
	$c_0 \leftarrow t \oplus r_{00}$
33 intermediate variables	$t \leftarrow a_0 \cdot b_1$
$\langle 22 \rangle$	$t \leftarrow t \oplus r_{01}$
$\binom{33}{2} = 528$ couples to verify	$c_0 \leftarrow c_0 \oplus t$
	$t \leftarrow a_0 \cdot b_2$
$\binom{n}{t}$ tuples to verify	$t \leftarrow t \oplus r_{02}$
	$c_0 \leftarrow c_0 \oplus t$
	$t \leftarrow a_1 \cdot b_0$
	$c_1 \leftarrow t \oplus r_{01}$
	$t \leftarrow a_1 \cdot b_1$
	$c_1 \leftarrow c_1 \oplus t$
	•••
	return (c_0, c_1, c_2)

Proof in the Random Probing Model

Reminder: an implementation is p-random probing secure iff the probability to get a tuple dependent from the secret is negligible given that each variable leaks with probability p

function example($a_0, a_1, a_2, b_0, b_1, b_2$)

$$\sum_{i=1}^{n} \binom{n}{i}$$
 tuples to verify

$$r_{00}, r_{01}, r_{02}, r_{12} \leftarrow \$$$

$$t \leftarrow a_0 \cdot b_0$$

$$c_0 \leftarrow t \oplus r_{00}$$

$$t \leftarrow a_0 \cdot b_1$$

$$t \leftarrow t \oplus r_{01}$$

$$c_0 \leftarrow c_0 \oplus t$$

$$t \leftarrow a_0 \cdot b_2$$

$$t \leftarrow t \oplus r_{02}$$

$$c_0 \leftarrow c_0 \oplus t$$

$$t \leftarrow a_1 \cdot b_0$$

$$c_1 \leftarrow t \oplus r_{01}$$

$$t \leftarrow a_1 \cdot b_1$$

$$c_1 \leftarrow c_1 \oplus t$$
...
return (c_0, c_1, c_2)

- Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret
- Two methods to verify t-probing security of small implementations
 - Theoretical proof from the structure of the algorithm
 - Automatic proofs with a tool



- Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret
- Two methods to verify t-probing security of small implementations
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for
$$i = 1$$
 to t do
 $r \leftarrow \$$
 $x_0 \leftarrow x_0 + r$
 $x_i \leftarrow x_i + r$
end for



- Reminder: an implementation is t-probing secure iff any set of at most t variables is independent from the secret
- Two methods to verify t-probing security of small implementations
 - Theoretical proof from the structure of the algorithm
 - Automatic proofs with a tool


Recent Automatic Tools

- maskVerif [1,2]
 - Originally built in 2015, then extended in 2019
 - Probing security
- CheckMasks [3]
 - In CommonLisp
 - Faster with some details on the algorithm structure
 - Probing security
- Bloem et al. [4]
 - Probing security with physical defaults

G. Barthe, S. Belaïd, F. Dupressoir, P.-A. Fouque, B. Grégoire, and P.-Y. Strub. Verified proofs of higher-order masking. EUROCRYPT 2015
 G. Barthe, S. Belaïd, G. Cassiers, P.-A. Fouque, B. Grégoire, and F.-X. Standaert. maskVerif: Automated Verification of Higher-Order Masking in Presence of Physical Defaults. ESORICS 2019

[3] J.-S. Coron. Formal verification of side-channel countermeasures via elementary circuit transformations. ACNS 2017

[4] R. Bloem, H. Groß, R. Iusupov, B. Könighofer, S. Mangard, and J. Winter. Formal verification of masked hardware implementations in the presence of glitches. EUROCRYPT 2018



Security order *t*





Security order *t*





function example(a_0, a_1, b_0, b_1) $r \leftarrow \$$ $u \leftarrow a_0 \cdot b_0$ $c_0 \leftarrow u \oplus r$ $v \leftarrow a_1 \cdot b_1$ $v \leftarrow v \cdot r$ $x \leftarrow a_0 \cdot b_1$ $w \leftarrow v \oplus x$ $z \leftarrow a_1 \cdot b_0$ $c_1 \leftarrow y \oplus z$ return (c_0, c_1)



Determine whether a tuple is independent from the secrets

function example(a_0, a_1, b_0, b_1) $r \leftarrow \$$ $u \leftarrow a_0 \cdot b_0$ $c_0 \leftarrow u \oplus r$ $v \leftarrow a_1 \cdot b_1$ $v \leftarrow v \cdot r$ $x \leftarrow a_0 \cdot b_1$ $w \leftarrow v \oplus x$ $z \leftarrow a_1 \cdot b_0$ $c_1 \leftarrow y \oplus z$ return (c_0, c_1)



Determine whether a tuple is independent from the secrets

$$w = a_1 \cdot b_1 \oplus r \oplus a_0 \cdot b_1$$

function example(
$$a_0, a_1, b_0, b_1$$
)
 $r \leftarrow \$$
 $u \leftarrow a_0 \cdot b_0$
 $c_0 \leftarrow u \oplus r$
 $v \leftarrow a_1 \cdot b_1$
 $v \leftarrow v \cdot r$
 $x \leftarrow a_0 \cdot b_1$
 $\textcircled{W} \leftarrow v \oplus x$
 $z \leftarrow a_1 \cdot b_0$
 $c_1 \leftarrow y \oplus z$
return (c_0, c_1)



- Determine whether a tuple is independent from the secrets
 - Rule I: secrets?

function example(a_0, a_1, b_0, b_1) $r \leftarrow \$$ $u \leftarrow a_0 \cdot b_0$ $c_0 \leftarrow u \oplus r$ $v \leftarrow a_1 \cdot b_1$ $v \leftarrow v \cdot r$ $x \leftarrow a_0 \cdot b_1$ $w \leftarrow v \oplus x$ $z \leftarrow a_1 \cdot b_0$ $c_1 \leftarrow y \oplus z$ return (c_0, c_1)



$$w = a_1 \cdot b_1 \oplus r \oplus a_0 \cdot b_1$$

- Determine whether a tuple is independent from the secrets
 - Rule I: secrets?
 - Rule 2: random values?

 $w = a_1 \cdot b_1 \oplus r \oplus a_0 \cdot b_1$

function example(
$$a_0, a_1, b_0, b_1$$
)
 $r \leftarrow \$$
 $u \leftarrow a_0 \cdot b_0$
 $c_0 \leftarrow u \oplus r$
 $v \leftarrow a_1 \cdot b_1$
 $v \leftarrow v \cdot r$
 $x \leftarrow a_0 \cdot b_1$
 $\textcircled{W} \leftarrow v \oplus x$
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return (c_0, c_1)



- Determine whether a tuple is independent from the secrets
 - Rule I: secrets?
 - Rule 2: random values?

w = r

function example(
$$a_0, a_1, b_0, b_1$$
)
 $r \leftarrow \$$
 $u \leftarrow a_0 \cdot b_0$
 $c_0 \leftarrow u \oplus r$
 $v \leftarrow a_1 \cdot b_1$
 $v \leftarrow v \cdot r$
 $x \leftarrow a_0 \cdot b_1$
 $\textcircled{W} \leftarrow v \oplus x$
 $z \leftarrow a_1 \cdot b_0$
 $c_1 \leftarrow y \oplus z$
return (c_0, c_1)



- Determine whether a tuple is independent from the secrets
 - Rule I: secrets?
 - Rule 2: random values?

w = r

- Go through all tuples
 - Verify bigger sets

function example(
$$a_0, a_1, b_0, b_1$$
)
 $r \leftarrow \$$
 $u \leftarrow a_0 \cdot b_0$
 $c_0 \leftarrow u \oplus r$
 $v \leftarrow a_1 \cdot b_1$
 $v \leftarrow v \cdot r$
 $x \leftarrow a_0 \cdot b_1$
 $\textcircled{W} \leftarrow v \oplus x$
 $z \leftarrow a_1 \cdot b_0$
 $c_1 \leftarrow y \oplus z$
return (c_0, c_1)



- Determine whether a tuple is independent from the secrets
 - Rule I: secrets?
 - Rule 2: random values?

w = r

- Go through all tuples
 - Verify bigger sets

Extensions

Extended probing model

function example(a_0, a_1, b_0, b_1) $r \leftarrow \$$ $u \leftarrow a_0 \cdot b_0$ $c_0 \leftarrow u \oplus r$ $v \leftarrow a_1 \cdot b_1$ $v \leftarrow v \cdot r$ $x \leftarrow a_0 \cdot b_1$ $w \leftarrow v \oplus x$ $z \leftarrow a_1 \cdot b_0$ $c_1 \leftarrow y \oplus z$ return (c_0, c_1)



- Examples of classical implementations
- Until 6 shares
- In the presence of glitches (HW)

	# obs		probing	
	HW	SW	HW	SW
first-order masking (2 shares)				
Trichina AND [33]	2	13	$0.01 \mathrm{s}$ X	0.01s X
ISW AND [25]	1	13	$0.01 \mathrm{s}$ X	0.01s
TI AND [32]	3	21	0.01s	0.01s
DOM AND [22]	4	13	0.01s	0.01s
DOM AND SNI	6	13	0.01s	0.01s
PARA AND [5]	6	16	0.01s	0.01s
DOM Keccak S-box [23]	20	76	0.01s	0.01s
DOM AES S-box [22]	96	571	0.06s	0.6s
TI Fides-160 S-box $[8]$	192	6657	0.3s	2.8s
TI Fides-192 APN [8]	128	69281	2.3s	3m49s
second-order masking (3 shares)				
DOM AND [22]	12	30	0.01s	0.01s
DOM AND SNI	15	30	0.01s	0.01s
PARA AND [5]	15	30	0.01s	0.01s
DOM Keccak S-box [23]	60	165	0.03s	0.03s
DOM AES S-box $[21]$	168	1205	10.7s	15m45s
third-order masking (4 shares)				
DOM AND [22]	20	54	0.02s	0.03s
DOM AND SNI	24	54	0.03s	0.03s
PARA AND NI [5]	20	48	0.02s	0.02s
PARA AND SNI [5]	28	53	0.02s	0.02s
DOM Keccak S-box [23]	100	290	0.49s	0.68s
DOM AES S-box [21]	296	2011	12m36s	∞
fourth-order masking (5 shares)				
DOM AND [22]	30	87	0.1s	0.1s
PARA AND NI [5]	35	75	0.18s	0.15s
PARA AND SNI [5]	40	85	0.16s	0.16s
DOM Keccak S-box [23]	150	450	20s	41s
fifth-order masking (6 shares)				
DOM Keccak S-box [23]	210	618	3m59s	14m6s





More efficient automatic verification tools





Main Challenges

More efficient automatic verification tools

Closer to the reality of embedded devices

- Takes implementations in Assembly language
- Proof in more accurate models





Composition





[1] Y. Ishai, A. Sahai, and D. Wagner. Private circuits: Securing hardware against probing attacks. CRYPTO 2003





[1] Y. Ishai, A. Sahai, and D. Wagner. Private circuits: Securing hardware against probing attacks. CRYPTO 2003

[2] M. Rivain and E. Prouff. Provably secure higher-order masking of AES. CHES 2010



- Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret
- How to reason on composition?





- Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret
- How to reason on composition?
 - Stronger property: non-interference

An implementation is t-non-interfering iff any set of at most t variables can be simulated with at most t input shares





























- Reminder: an implementation is *t*-probing secure iff any set of at most *t* variables is independent from the secret
- How to reason of composition?
 - Stronger property: non-interference

An implementation is t-non-interfering iff any set of at most t variables can be simulated with at most t input shares

Stronger property: strong non-interference

An implementation is t-strong non-interfering iff any set of

- tl internal variables
- t2 output variables

can be simulated with at most tI input shares





















Composition techniques

- Compose NI/SNI gadgets as shown
 - Tool maskComp
- Compose standard circuits in the probing model
 - Tool tightPROVE
 - Exact methods restricted to circuits from addition, ISW multiplications, and refresh gadgets
- Compose gadgets with stronger properties
 - Example: PINI



Main Challenges

Being able to compose any kind of gadgets without loss of efficiency





Main Challenges

Being able to compose any kind of gadgets without loss of efficiency

Compose in more realistic leakage models





Conclusion



Summary

- Side-channel attacks are very powerful
 - Few seconds to recover the key on some software devices
 - Cheap equipments


Summary

- Side-channel attacks are very powerful
 - Few seconds to recover the key on some software devices
 - Cheap equipments
- Masking is the most widely deployed countermeasure
 - Numerous works
 - Difficult to build secure constructions



Summary

- Side-channel attacks are very powerful
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Masking is the most widely deployed countermeasure

- Numerous works
- Difficult to build secure constructions

Verification

- Automatic tools
- Composition



Challenges

Efficiency

- The least possible randomness
- The least possible operations





Challenges

Efficiency

- The least possible randomness
- The least possible operations



Security

- Theoretical proofs of existing schemes
- Automatic tools to verify the security of implementations



Challenges

Efficiency

- The least possible randomness
- The least possible operations



Security

- Theoretical proofs of existing schemes
- Automatic tools to verify the security of implementations

Practicality

 Security of implementations under leakage models as close as possible to the reality



Thank you. Questions?

